

## Sorts

### 1) Selection

- a) Big O best case time -  $O(n^2)$
- b) Big O ave case time -  $O(n^2)$
- c) Big O worst case time -  $O(n^2)$
- d) worst case data set - reverse order
- e) space requirements - one vector
- f) other characteristics or comments - two nested loops, terribly, slow sort, inefficient for  $n > 100$  data sets, many comparisons, could be many assignments if in reversed order, only one swap per pass of the inner loop, no early exits

### 2) Bubble

- a) Big O best case time -  $O(n)$
- b) Big O ave case time -  $O(n^2)$
- c) Big O worst case time -  $O(n^2)$
- d) worst case data set - reverse order since a lot of values must "bubble down"
- e) space requirements - one vector
- f) other characteristics or comments - two nested loops (for nested in a while typically) with early exit in the outer loop, good when the data is mostly sorted to start with, could cause a lot of swaps

### 3) Insertion

- a) Big O best case time -  $O(n)$
- b) Big O ave case time -  $O(n^2)$
- c) Big O worst case time -  $O(n^2)$
- d) worst case data set - reverse order
- e) space requirements - only one vector if you are efficient but commonly done with two vectors (1 unsorted, other sorted), two nested loops
- f) other characteristics or comments - good when the data is mostly sorted to start with, absolutely terrible in many cases, aka poker hand sort, early exit from inner loop

### 4) Shell

- a) Big O best case time -  $O(n(\log n)^2)$
- b) Big O ave case time -  $O(n(\log n)^2)$
- c) Big O worst case time - between  $O(n^1)$  and  $O(n^2)$  (but closer to  $O(n^2)$ )
- d) worst case data set - reverse order
- e) space requirements - one vector
- f) other characteristics or comments - the "inner sort" of the partition elements which are separated by a gap can be performed with whatever sorting algorithm you wish (our author uses an insertion sort, aka a diminishing increment sort, best case is when successive gap sizes are relatively prime)

### 5) Quick

- a) Big O best case time -  $O(n \log n)$
- b) Big O ave case time -  $O(n \log n)$
- c) Big O worst case time -  $O(n^2)$
- d) worst case data set - when data is already ordered and when poor pivot values are chosen
- e) space requirements - Big O for space is  $O(n)$  in worst case, one vector in each recursive stack frame
- f) other characteristics or comments - may be worthwhile to randomize the data so that data is not close to sorted before using quick sort

### 6) Heap

- a) Big O best case time -  $O(n \log n)$
- b) Big O ave case time -  $O(n \log n)$
- c) Big O worst case time -  $O(n \log n)$

- d) worst case data set - more swaps if data is in reverse order, but no real worst case
- e) space requirements - one vector though in some implementations people use two vectors (one for the heap and one for the sorted values)
- f) other characteristics or comments - two phases to this algorithm: putting values into a heap (i.e. binary tree with the heap property) and then "picking" the sorted values out of the heap one-by-one

7) Merge

- a) Big O best case time -  $O(n \log n)$
- b) Big O ave case time -  $O(n \log n)$
- c) Big O worst case time -  $O(n \log n)$
- d) worst case data set - none
- e) space requirements - high,  $\log n$  recursive stack frames each with a separate vector
- f) other characteristics or comments - good to use if data compared to the quick sort if the data is almost sorted

8) Radix

- a) Big O best case time -  $O(n)$
- b) Big O ave case time -  $O(n)$
- c) Big O worst case time -  $O(n)$
- d) worst case data set - if data elements are large it will consume a lot of memory
- e) space requirements - excessive
- f) other characteristics or comments - not suitable for all types of data such as floating-point values, has a large constant of proportionality despite being  $O(n)$